



CS 149

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Clarity With If-Else

Imagine we are working on a game application that requires us to determine when the player has won. Players win when their score *exceeds* 100 points. Here are five possible implementations (assume that `win` is declared as a boolean variable.)

```
// A
if (points > 100) {
    win = true;
} else if (points < 100){
    win = false;
}
```

```
// B
if (points > 100) {
    win = true;
} else if (points <= 100){
    win = false;
}
```

```
// C
if (points > 100) {
    win = true;
} else {
    win = false;
}
```

```
// D
if (points > 100) {
    win = true;
}
if (points < 100){
    win = false;
}
```

```
// E
win = points > 100;
```

If-Else Exercise 1

1. Complete the table below with the value of win that will result from each of the implementations above. Every entry should be `true` or `false`.

	<code>points == 99</code>	<code>points == 100</code>	<code>points == 101</code>
A			
B			
C			
D			
E			

2. Which of these five implementations are correct?
3. Of the correct implementations, which is easiest to understand? Why?



Recursion

"In mathematics, the *factorial* of a non-negative integer n , denoted by $n!$, is the product of all positive integers less than or equal to n . For example, $5! = 5 \times 4 \times 3 \times 2 \times 1 = 120$." Source: <https://en.wikipedia.org/wiki/Factorial>

n	$n!$
0	1
1	1
2	2
3	6
4	24
5	120

- Consider how to calculate $4! = 24$.
 - Write out all the numbers that need to be multiplied:
 $4! =$
 - Rewrite the expression using $3!$ instead of $3 \times 2 \times 1$:
 $4! =$
- Write an expression similar to #1b showing how each factorial can be calculated in terms of a simpler factorial.
 - $3! =$
 - $2! =$
 - $100! =$
 - $n! =$
- What is the value of $0!$ based on the model? Does it make sense to define $0!$ in terms of a simpler factorial? Why or why not?

*If we repeatedly break down a problem into smaller versions of itself, we eventually reach a basic problem that can't be broken down any further. Such a problem, like $0!$, is referred to as the **base case**.*

Recursion Trace

```
1 public static int factorial(int n) {
2     System.out.println("n is " + n);
3     if (n == 0) {
4         return 1; // base case
5     } else {
6         System.out.printf("need factorial of %d\n", n - 1);
7         int answer = factorial(n - 1);
8         System.out.printf("factorial of %d is %d\n", n - 1, answer);
9         return n * answer;
10    }
11 }
12
13 public static void main(String[] args) {
14     System.out.println(factorial(3));
15 }
```



Recursion Trace questions

- a) What specific method is invoked on line 7?
- b) Why is the if statement required on line 3?



Recursion - Factorials

- A method that invokes itself is called **recursive**. What two steps were necessary to define factorial? How were they implemented in Java?
- 7. How many distinct method calls would be made to factorial to compute the factorial of 3? Identify the value of the parameter n for each of these separate calls.
- 8. Here is the complete output from the program in #5. Identify which distinct method call printed each line. In other words, which lines were printed by factorial(3), which lines were printed by factorial(2), and so on.

```
n is 3
need factorial of 2
n is 2
need factorial of 1
n is 1
need factorial of 0
n is 0
factorial of 0 is 1
factorial of 1 is 1
factorial of 2 is 2
6
```

- 9. What happens if you try to calculate the factorial of a negative number? How could you prevent this bug in the factorial method?

- **Acknowledgements**

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